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# Towards Robustness to Different Types of Concept Drift in Data Stream Learning

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**EPSRC**

SPDISC  
*Project*

# Outline

- Motivation and definitions.
  - Example applications.
  - Data stream.
  - Online learning.
  - Concept drift.
  - Types of concept drift.
- A diversity framework based on clustering in the model space.
  - Diversity.
  - Using diversity as a memory strategy.
  - Clustering in the model space to compose a more robust ensemble.
  - Evaluation.
- Other challenges in learning under concept drift.
  - Partially labelled data.
  - Verification latency.
  - Lack of data from target domain.
  - Novel regions of the input space.
  - Class evolution.
  - Class imbalance.





1.15 million inhabitants; 2nd largest city in the UK.



Founded in 1825.

# My Lab

## Software Engineering

- Software Defect Prediction
- Software Effort Estimation
- Software Project Scheduling

## Artificial Intelligence

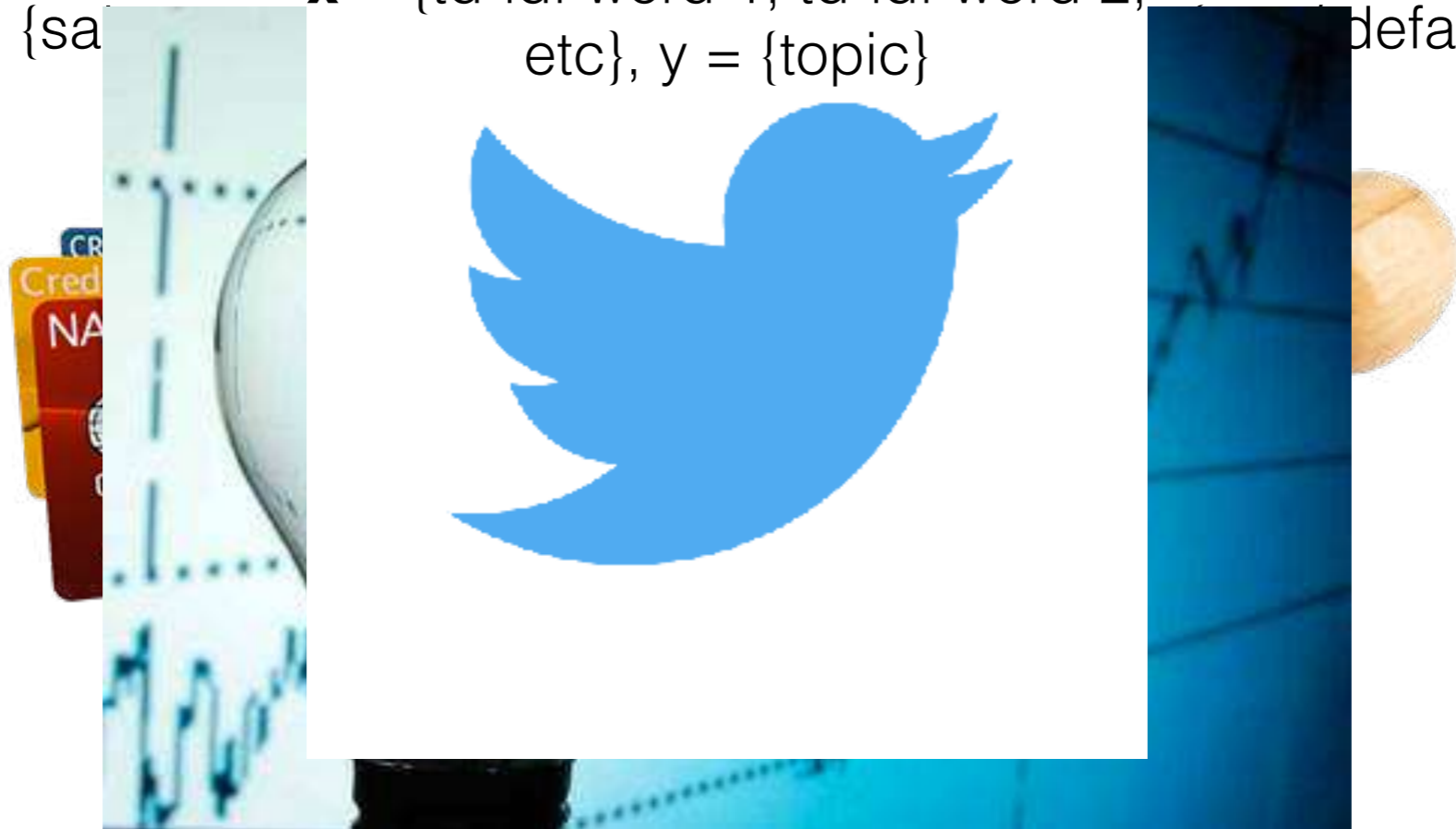
- Learning in Dynamic Environments
- Class Imbalance Learning
- Transfer Learning
- Ensemble Learning
- Evolutionary Algorithms

# Data Stream Learning of Classification Problems

**Data stream:** ordered and potentially infinite sequence of examples  $\mathcal{S} = \{(\mathbf{x}^{(1)}, y^{(1)}), (\mathbf{x}^{(2)}, y^{(2)}), \dots\}$  where  $(\mathbf{x}^{(t)}, y^{(t)}) \in \mathcal{X} \times \mathcal{Y}$ ,  $(\mathbf{x}^{(t)}, y^{(t)}) \sim p^{(t)}(\mathbf{x}, y)$ .

$\mathbf{x} = \{\text{demand, day of week, etc}\}, y =$

$\mathbf{x} = \{\text{sa}, \text{td-idf word 1, td-idf word 2, etc}\}, y = \{\text{topic, default}\}$



# Online Supervised Learning of Classification Problems

- Given a model  $f^{(t-1)} : \mathcal{X} \rightarrow \mathcal{Y}$  and a new example  $(\mathbf{x}^{(t)}, y^{(t)})$  from a probability distribution  $p^{(t)}(\mathbf{x}, y)$ .
- Learn a model  $f^{(t)} : \mathcal{X} \rightarrow \mathcal{Y}$  able to generalise to unseen examples of the distribution  $p^{(t)}(\mathbf{x}, y)$ .
- **Strict online learning:** only  $f^{(t-1)}$  and  $(\mathbf{x}^{(t)}, y^{(t)})$  are available for learning.
- **Non-strict scenarios:**  $f^{(t-1)}$ ,  $(\mathbf{x}^{(t)}, y^{(t)})$  and a limited number of past examples may be available.



# Concept Drift

- **Concept drift**: a change in the joint probability distribution
  - $p^{(t)}(\mathbf{x}, y) = p^{(t)}(y | \mathbf{x})p^{(t)}(\mathbf{x})$

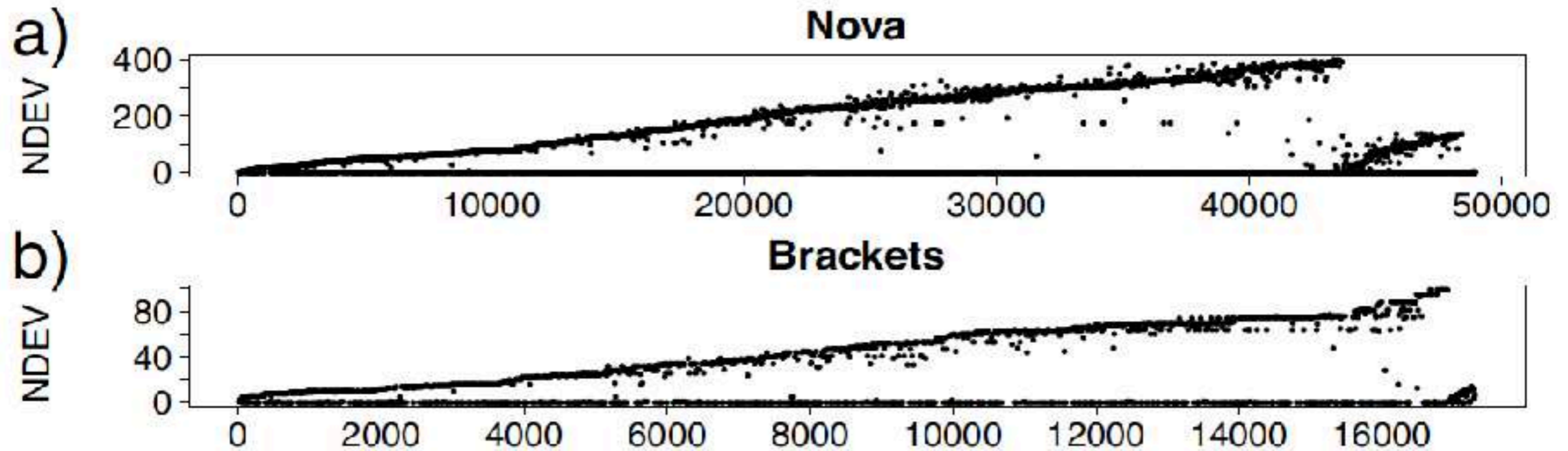


E.g.: credit card approval being affected by economic crises.

# Concept Drift

- **Concept drift**: a change in the joint probability distribution
  - $p^{(t)}(\mathbf{x}, y) = p^{(t)}(y | \mathbf{x})p^{(t)}(\mathbf{x})$

Number of developers that changed the modified files (NDEV) over time



# Characterisation of Concept Drifts

- **Severity or magnitude:** size of the changes caused by the concept drift.
- Proportion of the input space that has its target class changed.

$$\int I(p^{(t)}(y|\mathbf{x}) \neq_e p^{(t')}(y|\mathbf{x})) d\mathbf{x}$$

L. Minku, A. White and X. Yao. The Impact of Diversity on On-line Ensemble Learning in the Presence of Concept Drift, IEEE Transactions on Knowledge and Data Engineering 22(5):730-742, 2010.

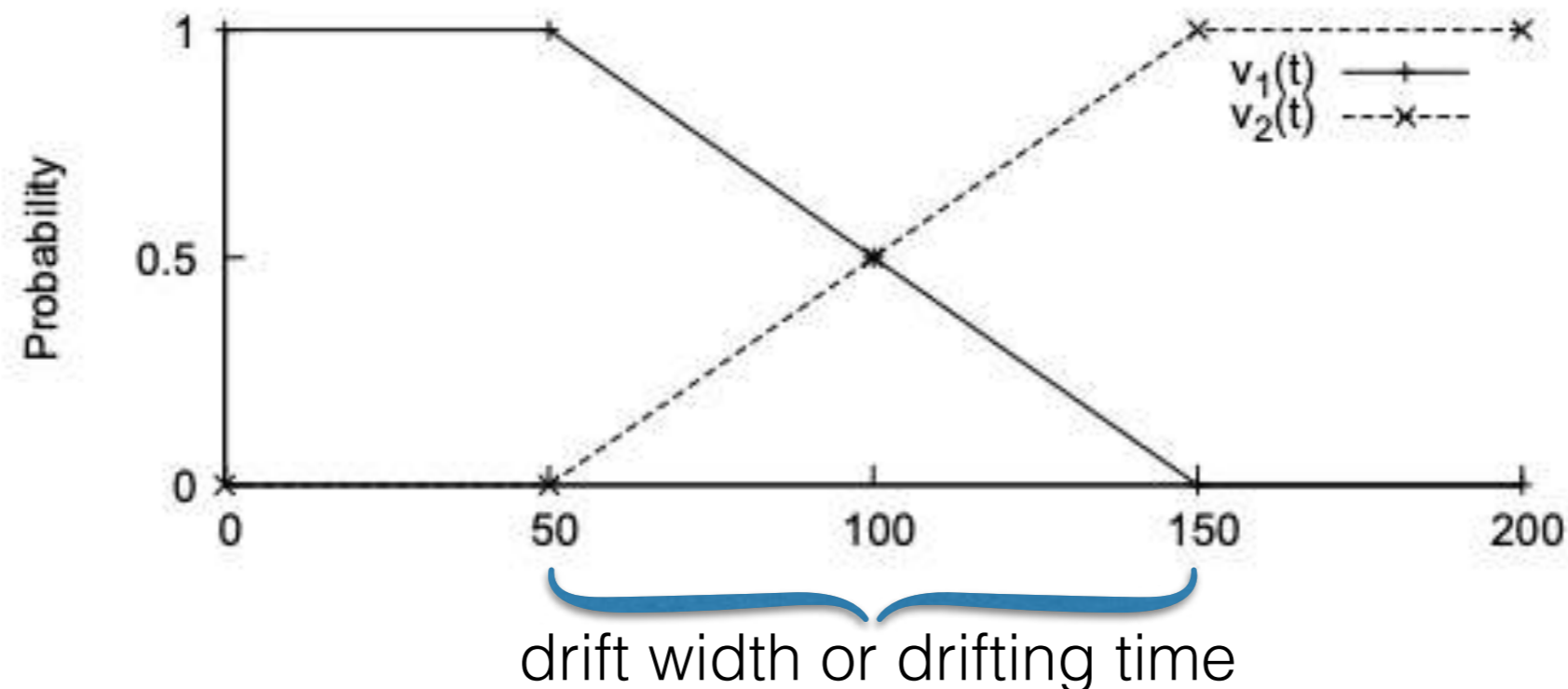
- Distance between distributions, e.g., Hellinger distance.

$$H^2(p^{(t)}, p^{(t')})$$

G. Webb et al. Characterising Concept Drift. Data Mining and Knowledge Discovery 30:964-994, 2016.

# Characterisation of Concept Drifts

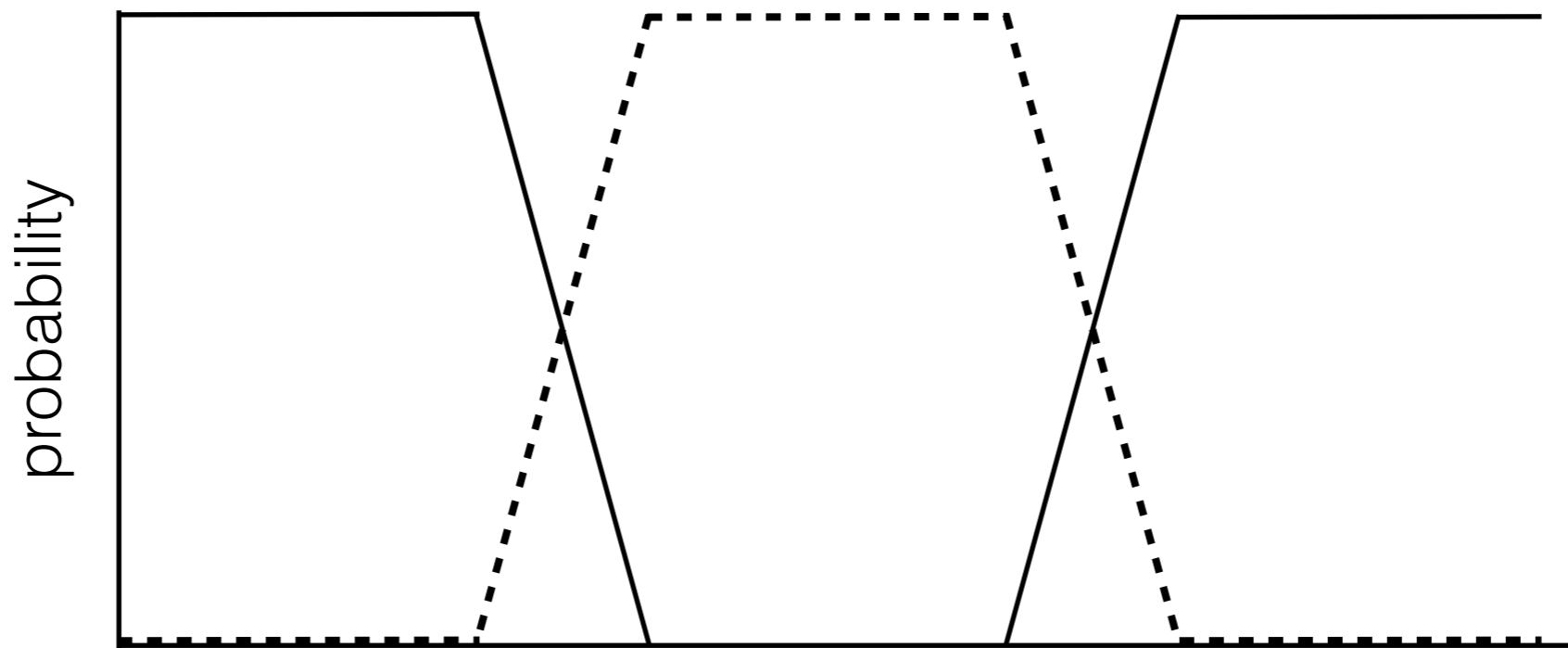
- **Speed**: how fast the new probability distribution replaces the past one.
  - **Abrupt drifts**: replace current distribution suddenly.
  - **Gradual**: replace current distribution slowly.



L. Minku, A. White and X. Yao. The Impact of Diversity on On-line Ensemble Learning in the Presence of Concept Drift, IEEE Transactions on Knowledge and Data Engineering 22(5):730-742, 2010.

# Characterisation of Concept Drifts

- **Recurrence:** whether the joint probability distribution reoccurs over time.
- A new joint probability distribution may also be similar, but not the same as a past distribution.



L. Minku, A. White and X. Yao. The Impact of Diversity on On-line Ensemble Learning in the Presence of Concept Drift, IEEE Transactions on Knowledge and Data Engineering 22(5):730-742, 2010.

# Online Approaches for Concept Drift Handling

- Abrupt drifts:
  - Typically best dealt with based on explicit (active) approaches:
    - Make use of an explicit concept drift detection method.
    - Special adaptation mechanisms are triggered upon concept drift detection.
- Gradual drifts:
  - Typically best dealt with based on implicit (passive) approaches:
    - Do not make use of an explicit concept drift detection method.
    - Continuously attempt to adapt to the current distribution.
    - Most of such approaches are ensemble approaches.

G. Ditzler et al. Learning in Nonstationary Environments: a survey, IEEE Computational Intelligence Magazine 10(4):12-25, 2015.

B. Krawczyk et al. Ensemble Learning for Data Stream Analysis: a survey, Information Fusion 37:132-156, 2017.

# Online Approaches for Concept Drift Handling

- Recurrent drifts:
  - Memory-based approaches can help to deal with recurrent drifts.
    - Single learners retrieved from the memory.
    - Ensembles.
- Severe / not severe drifts:
  - Approaches typically depend on hyperparameters to control the trade-off between sensitivity to noise and ability to deal with drifts of different severities.

## How to improve robustness to different types of concept drift?

C. Chiu, L. Minku. A Diversity Framework for Dealing with Multiple Types of Concept Drift Based on Clustering in the Model Space. [IEEE Transactions on Neural Networks and Learning Systems](#), 2020 (in press).





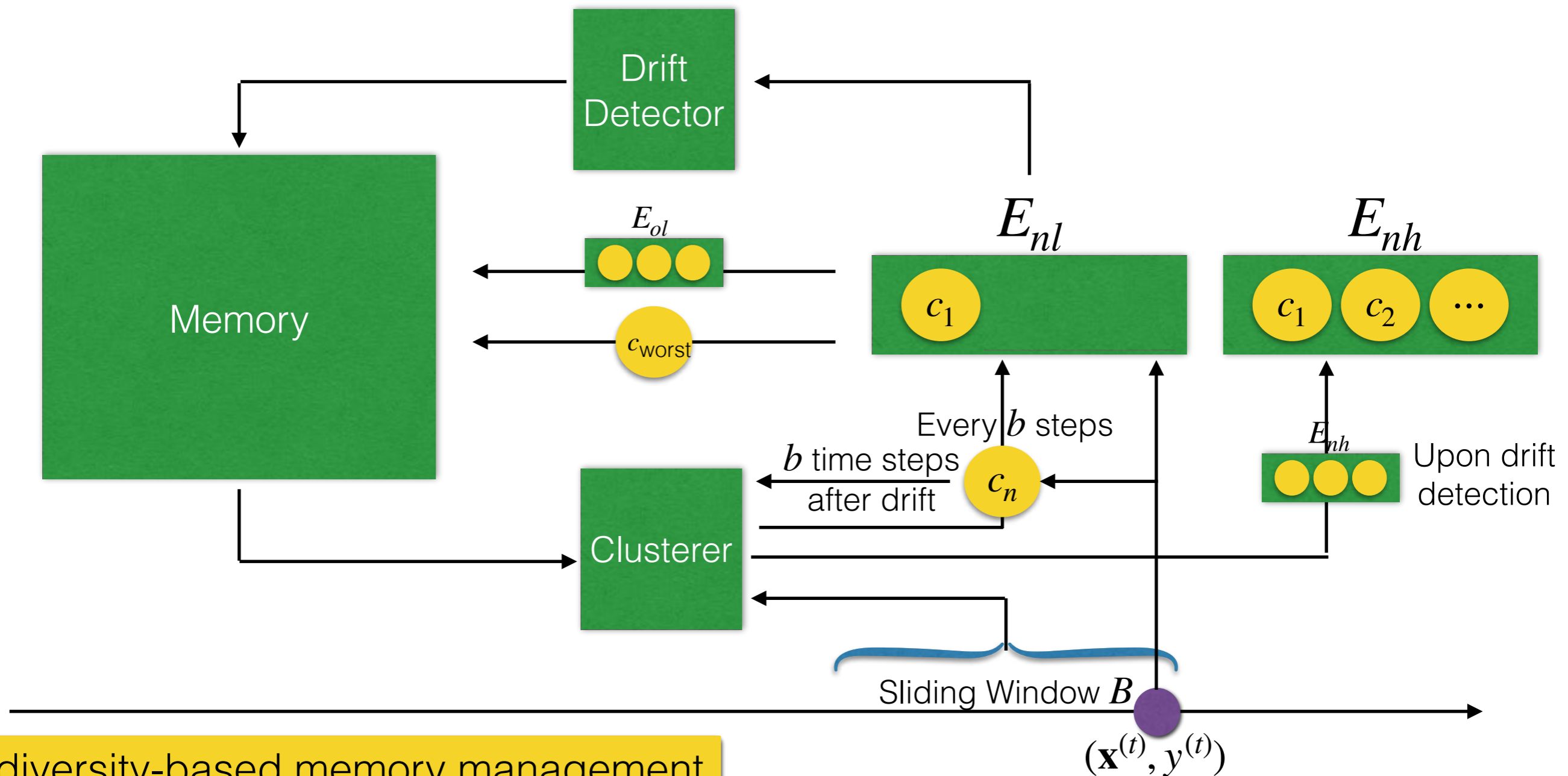
# Diversity and Clustering in the Model Space

- Diversity is the level of disagreement among different models. E.g., Q-statistic:

$$Q_{i,k} = \frac{N^{11}N^{00} - N^{01}N^{10}}{N^{11}N^{00} + N^{01}N^{10}}$$

- Diversity can potentially work as a memory management strategy to maintain a **diverse memory of previous models**, increasing the chances that relevant past models are kept.
- Clustering the memory models can help to decide **which models to retrieve** from the memory to deal with various types of drift.
- No previous work had exploited the full potential of diversity as a memory strategy to increase robustness to different types of drift.

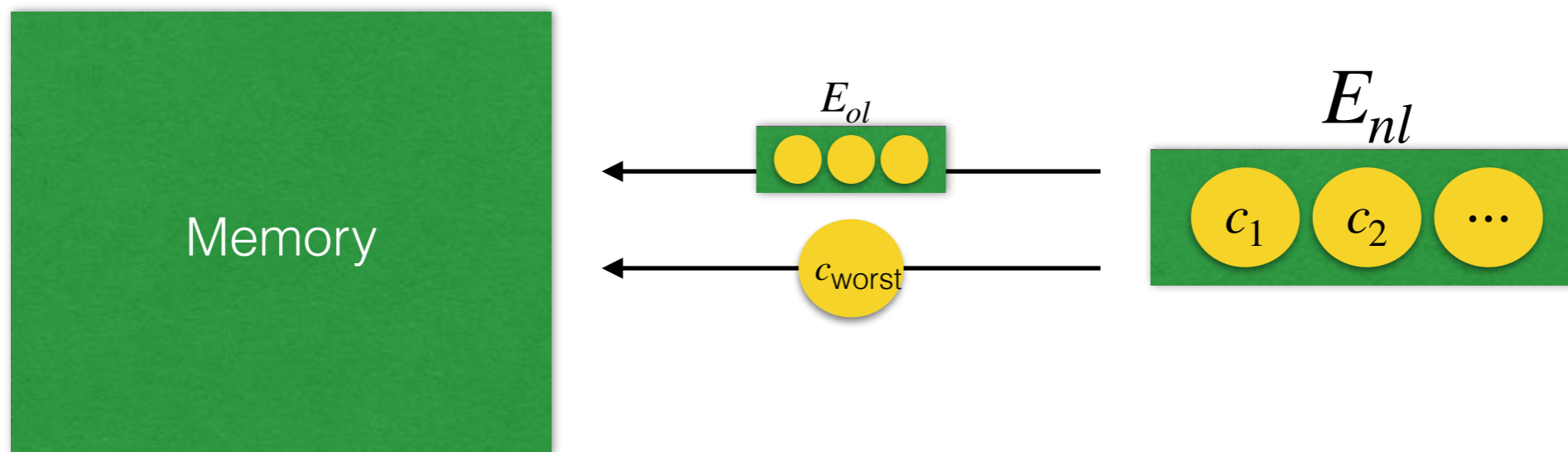
# Concept Drift Handling Based on Clustering in the Model Space (CDCCMS)



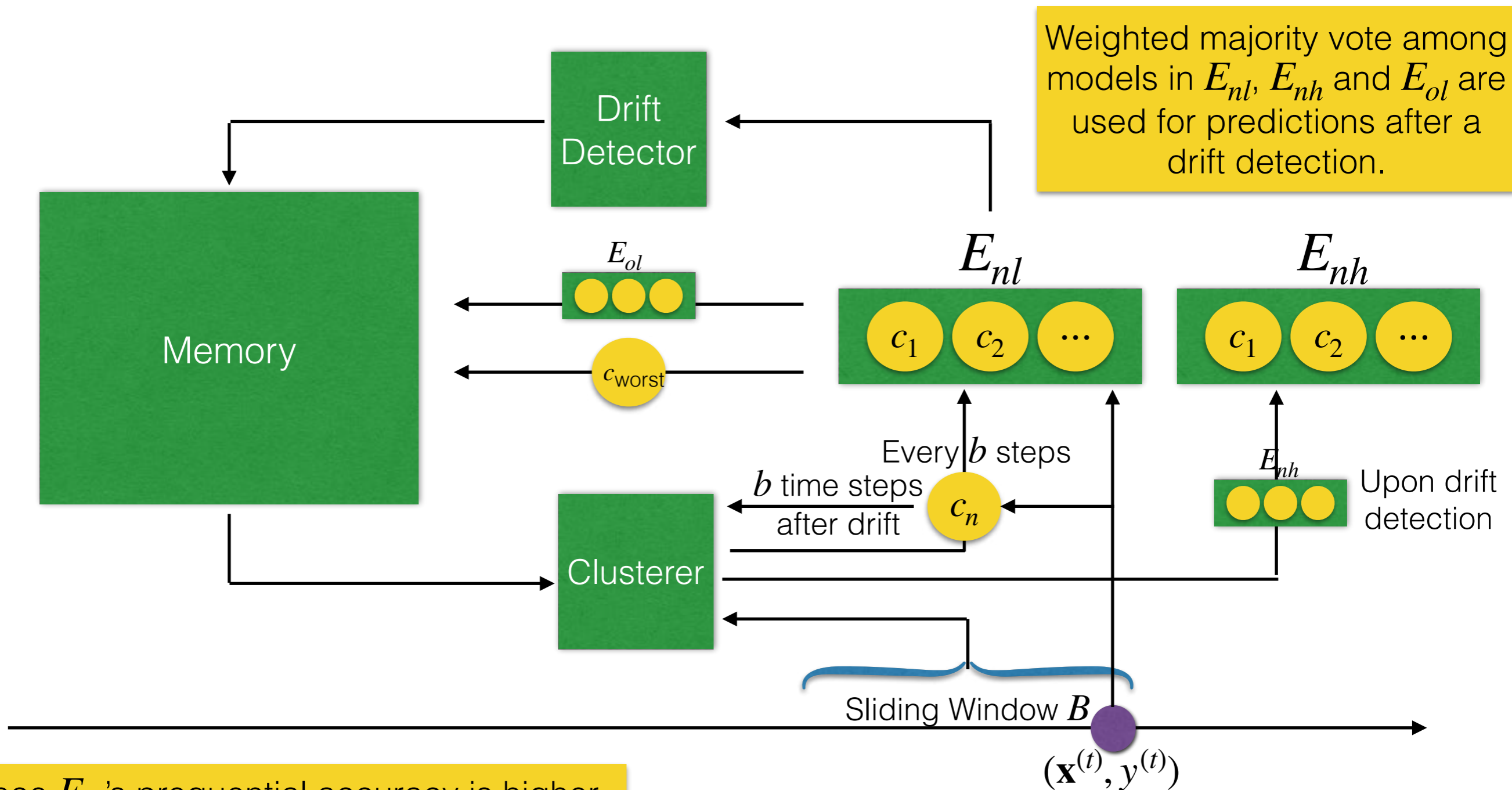
A diversity-based memory management strategy is used to decide which model to keep in the memory.

# Diversity-Based Memory Maintenance

- If the memory is full, a model will be deleted from it.
- The model to be deleted is the most similar one to the model being added, according to the diversity metric  $Q$ .
- Maintaining a diverse memory is key to deal with recurrent drifts or any drifts that may benefit from past knowledge.



# Concept Drift Handling Based on Clustering in the Model Space (CDCCMS)



# Synthetic Datasets

TABLE I  
DATA STREAMS

Data Stream	Concept Drift Sequence
Sine1	f3 → f4 → f3
Sine2	f1 → f2 → f3 → f4 → f1
Agr1	f1 → f3 → f4 → f7 → f10
Agr2	f7 → f4 → f6 → f5 → f2 → f9
Agr3	f4 → f2 → f1 → f3 → f4
Agr4	f1 → f3 → f6 → f5 → f4
SEA1	f5 → f3 → f1 → f2 → f4
SEA2	f5 → f1 → f4 → f3 → f2
STA1	f1 → f2 → f3 → f2
STA2	f2 → f3 → f1 → f2

Coloured rows (lime / light grey) highlight data streams with recurring concepts.  $f_n$  represents the n-th function of the stream type, i.e., f1 in Agr1 is referring to the first function of the Agrawal generator.

Abrupt and gradual with width of 2000 time steps.

# Synthetic Datasets

TABLE II  
PERCENTAGE DIFFERENCE OF CONCEPTS

		Sine			SEA				STAGGER	
	f1	f2	f3	f1	f2	f3	f4	f1	f2	
f2	100.0%	-	-	8.5%	-	-	-	59.3%	-	
f3	26.8%	73.2%	-	7.4%	16.0%	-	-	77.8%	48.1%	
f4	73.2%	26.8%	100.0%	13.1%	4.6%	20.6%	-	-	-	
f5	-	-	-	23.9%	32.5%	16.5%	37.1%	-	-	

		Agrawal								
	f1	f2	f3	f4	f5	f6	f7	f8	f9	
f2	53.9%	-	-	-	-	-	-	-	-	
f3	53.1%	50.8%	-	-	-	-	-	-	-	
f4	53.9%	20.5%	50.8%	-	-	-	-	-	-	
f5	53.4%	47.6%	50.7%	47.7%	-	-	-	-	-	
f6	69.9%	28.9%	51.2%	35.5%	48.1%	-	-	-	-	
f7	50.5%	53.3%	50.1%	53.5%	60.1%	57.2%	-	-	-	
f8	33.5%	60.4%	46.5%	59.6%	59.6%	59.8%	49.8%	-	-	
f9	50.4%	53.3%	50.2%	53.5%	59.9%	57.3%	6.0%	49.5%	-	
f10	32.9%	61.3%	46.5%	61.3%	60.0%	59.9%	51.1%	1.8%	51.1%	

$$diff(f_a, f_b) = \sum_{i=1}^n \frac{|y_{fa}^{(i)} - y_{fb}^{(i)}|}{n} \quad \text{where } n = 1m$$

# Real World Datasets

- KDD Cup 99 — network intrusion detection. Ps: the drifts themselves are not real.
- Power supply — predict which hour the power supply comes from.
- Sensor — predict which sensor the temperature, humidity, light and voltage comes from.

Data streams available at: <https://www.cse.fau.edu/~xqzhu/stream.html>

# Baseline Approaches

- HTNB: Hoeffding tree with naive Bayes in the leaves.

P. Domingos and G. Hulten, "Mining High-Speed Data Streams," ACM SIGKDD, 11 2002.

- DDD: diversity-based explicit ensemble approach (not prepared for recurrent drifts).

L. L. Minku and X. Yao, DDD: A New Ensemble Approach for Dealing with Concept Drift, IEEE TKDE 24: 619–633, 2012.

- DP: diverse memory explicit approach for recurrent drifts (not prepared for gradual drifts).

C. W. Chiu and L. L. Minku, Diversity-Based Pool of Models for Dealing with Recurring Concepts, IJCNN, pp. 2759–2766, 2018.

- RCD: memory-based explicit approach for recurrent drifts (based on FIFO management strategy).

J. Goncalves Jr and R. Barros, RCD: A Recurring Concept Drift Framework, Patt. Recognit. Lett., 34:1018–1025, 2013.

- OAUE: implicit ensemble approach (delete worst as memory management strategy).

D. Brzezinski and J. Stefanowski, Combining Block-based and Online Methods in Learning Ensembles from Concept Drifting Data Streams, Information Sciences, 265:50–67, 2014



# Accuracy on Synthetic Data Streams with Gradual Drifts

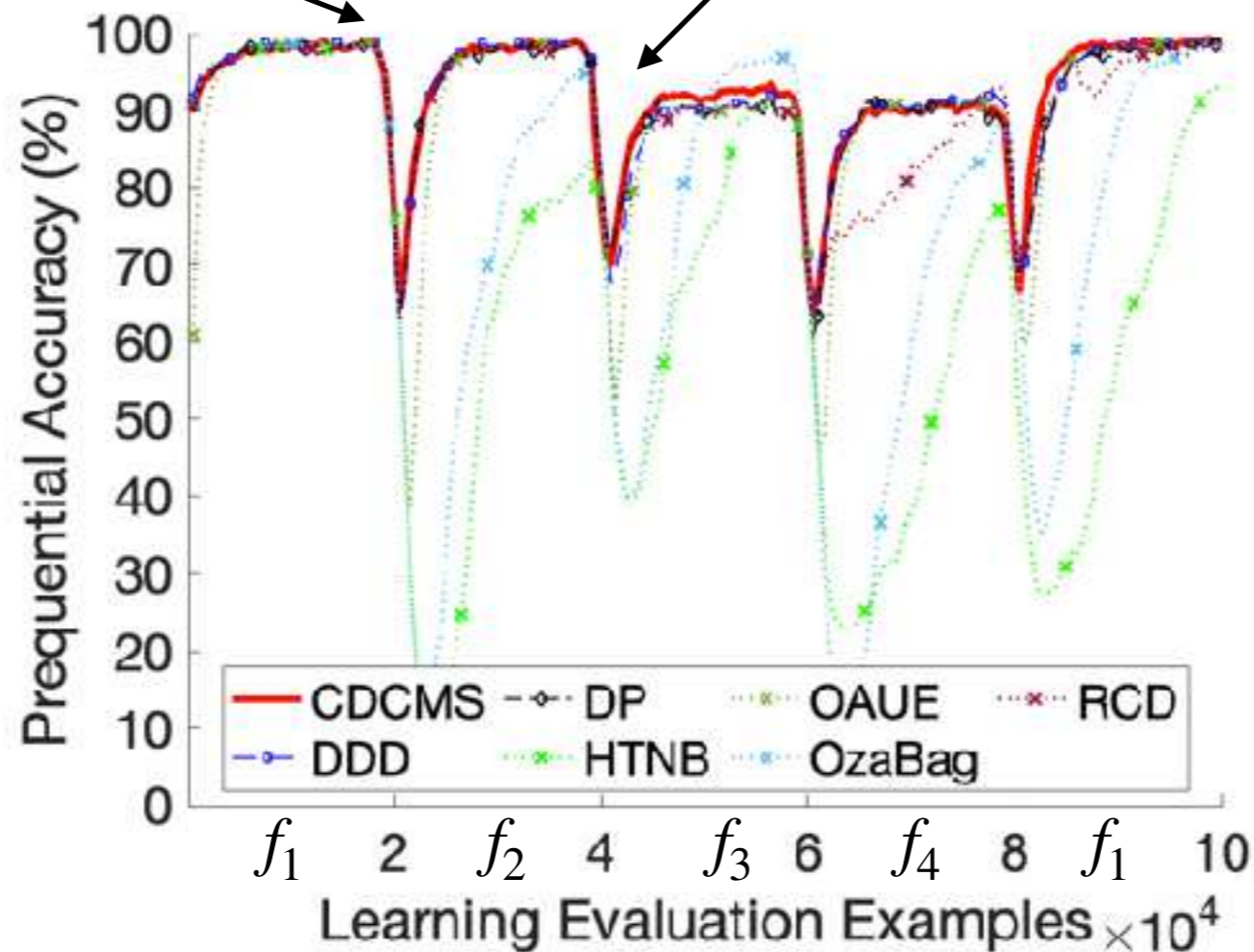
Data Stream	Synthetic Data Stream with <b>Gradual</b> Drifts						
	CDCMS	HTNB	OzaBag	DP	OAUE	RCD	DDD
Sine1	87.737% (6.109%)	67.745% (22.178%)	75.283% (23.252%)	<b>88.3%</b> <b>(5.958%)</b>	85.92% (9.998%)	87.806% (6.026%)	<b>87.786%</b> <b>(7.341%)</b>
Sine2	<b>92.692%</b> <b>(7.666%)</b>	65.555% (26.393%)	74.39% (26.552%)	<b>91.689%</b> <b>(7.935%)</b>	89.968% (12.008%)	90.39% (8.643%)	<b>91.632%</b> <b>(9.236%)</b>
Agr1	<b>89.53%</b> <b>(8.576%)</b>	74.003% (11.758%)	71.998% (12.03%)	85.268% (10.152%)	<b>89.707%</b> <b>(9.193%)</b>	85.634% (8.302%)	87.293% (10.867%)
Agr2	<b>78.494%</b> <b>(11.311%)</b>	67.301% (12.327%)	68.304% (12.175%)	71.877% (9.767%)	<b>80.458%</b> <b>(9.153%)</b>	73.954% (10.229%)	74.09% (11.955%)
Agr3	<b>82.895%</b> <b>(9.108%)</b>	70.068% (8.178%)	70.295% (8.731%)	75.833% (7.616%)	<b>83.413%</b> <b>(9.116%)</b>	78.58% (9.037%)	77.759% (10.457%)
Agr4	<b>81.187%</b> <b>(11.45%)</b>	69.749% (14.208%)	67.592% (14.072%)	75.46% (12.894%)	<b>82.505%</b> <b>(10.119%)</b>	77.783% (11.093%)	77.647% (13.051%)
SEA1	<b>87.591%</b> <b>(1.488%)</b>	86.117% (2.239%)	86.581% (2.777%)	86.879% (1.709%)	87.168% (2.505%)	86.71% (1.855%)	<b>87.525%</b> <b>(1.652%)</b>
SEA2	<b>86.841%</b> <b>(1.652%)</b>	85.036% (3.392%)	85.733% (3.62%)	86.296% (1.854%)	<b>86.713%</b> <b>(2.579%)</b>	86.033% (1.965%)	<b>86.738%</b> <b>(1.964%)</b>
STA1	<b>98.268%</b> <b>(4.193%)</b>	86.462% (14.325%)	86.782% (13.774%)	<b>98.183%</b> <b>(4.306%)</b>	96.898% (7.258%)	97.783% (4.91%)	<b>98.132%</b> <b>(4.466%)</b>
STA2	<b>98.155%</b> <b>(4.623%)</b>	78.25% (16.809%)	78.511% (16.635%)	<b>98.079%</b> <b>(4.65%)</b>	96.842% (7.484%)	97.713% (5.402%)	97.949% (5.028%)

Bold font shows top ranked methods based on Friedman and Nemenyi tests at level of significance of 0.05.

# Sample Gradual Drift Results

Drift detection leading to new unseen distribution (severity 100%)

Drift detection recovering  $f_1$  (difference 26.8%)

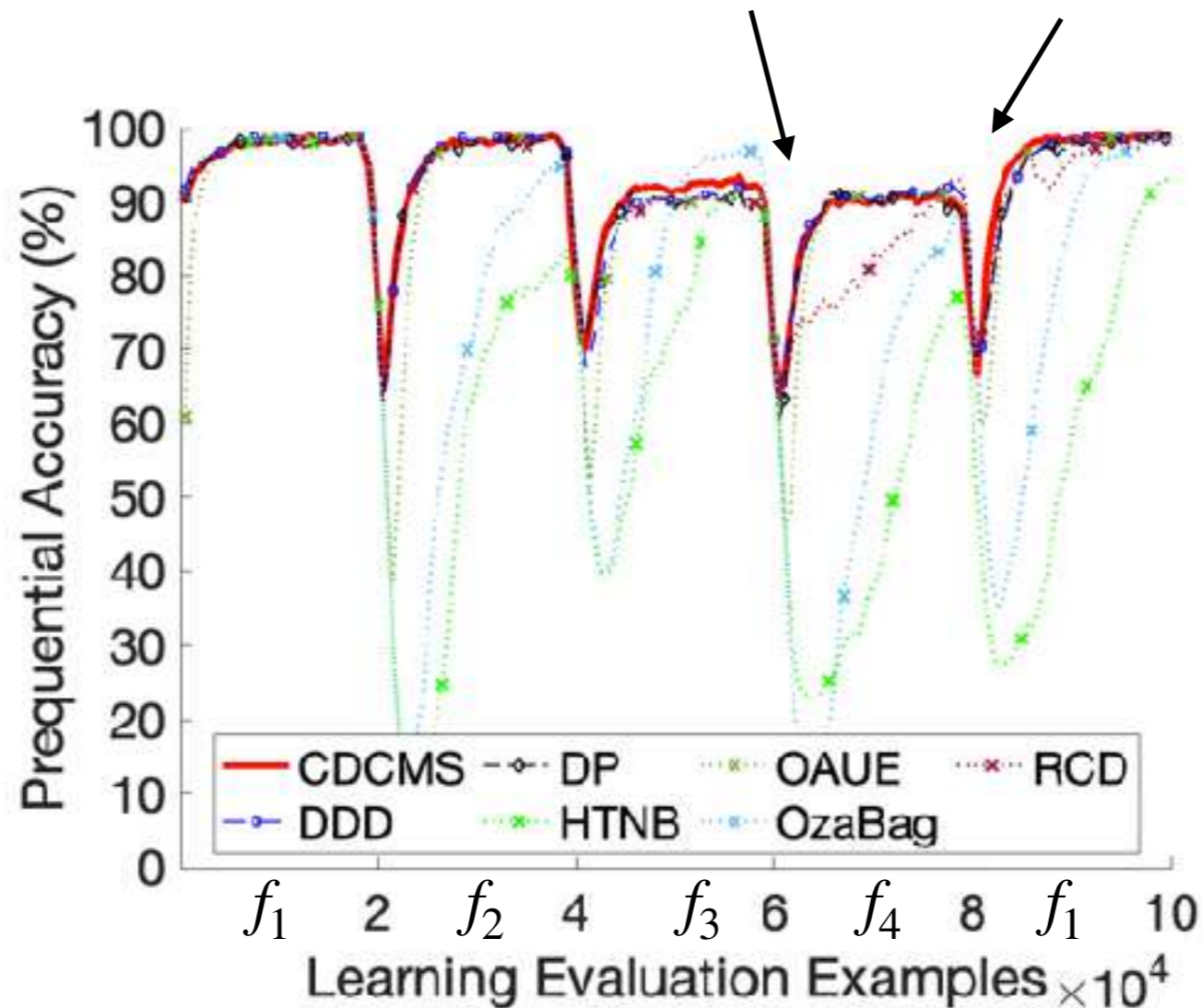


Sin2 - Gradual

# Sample Gradual Drift Results

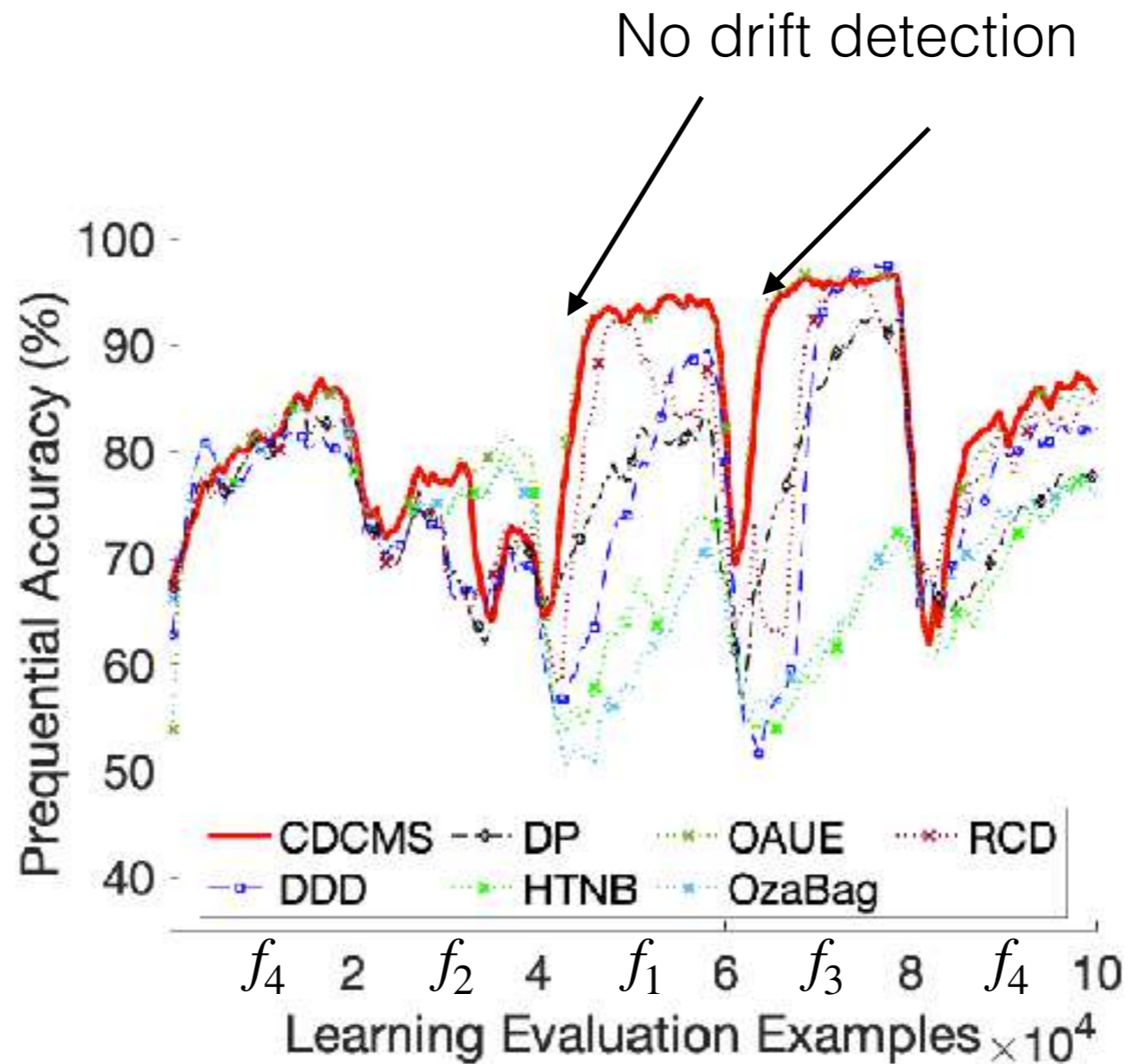
Drift detection recovering  $f_1$  and  $f_2$   
(difference 73.2% and 26.8%)

Drift detection recovering  $f_1$



Sin2 - Gradual

# Sample Gradual Drift Results

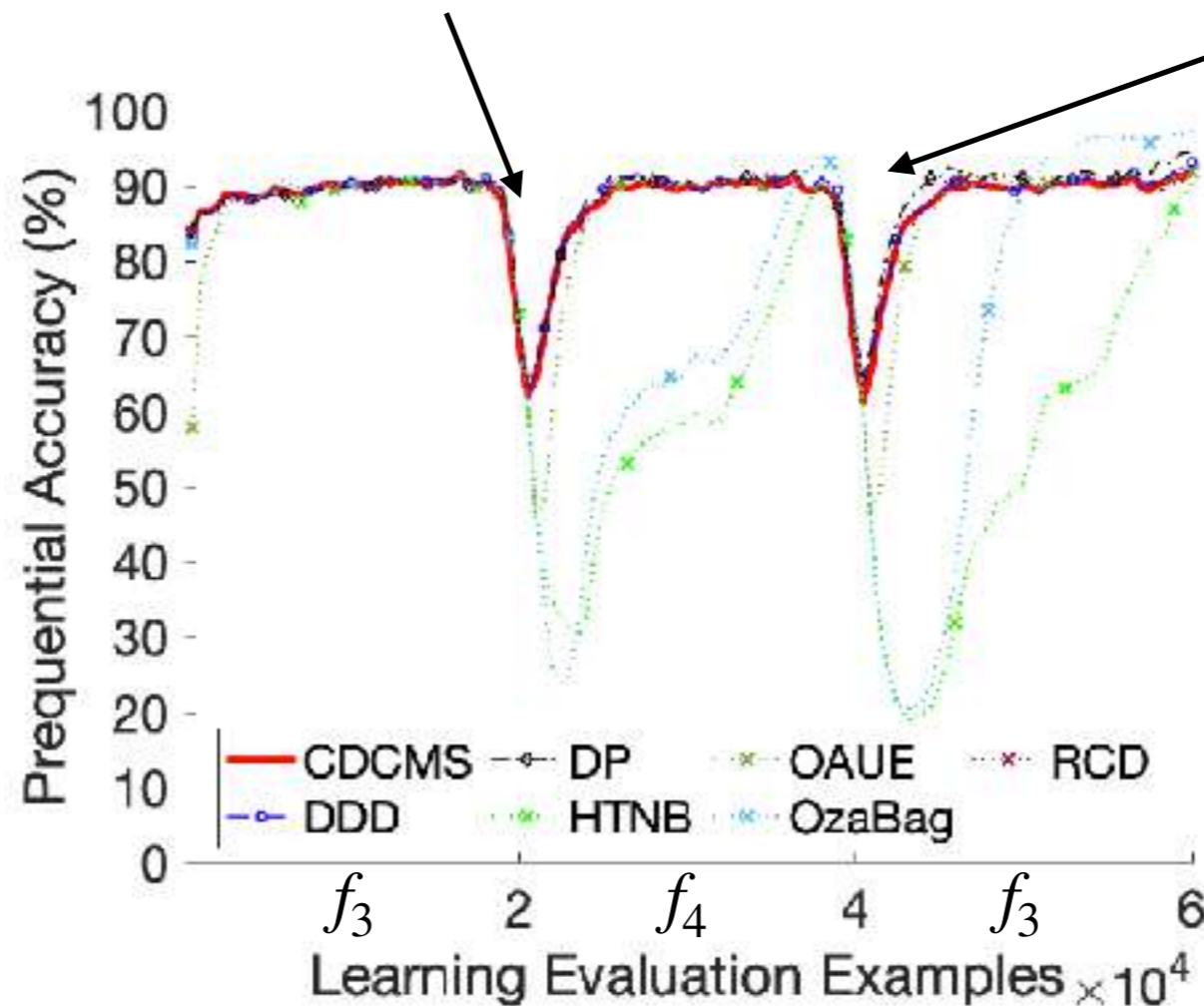


Agr3 - Gradual

# Sample Gradual Drift Results

False positive drift detection  
learning an intermediate distribution

Recovering intermediate  
model, instead of pure model



Sin1 - Gradual

# Accuracy on Synthetic Data Streams with Abrupt Drifts

Data Stream	Synthetic Data Stream with Abrupt Drifts						
	CDCMS	HTNB	OzaBag	DP	OAUE	RCD	DDD
Sine1	<b>90.248%</b> (1.586%)	74.35% (18.25%)	78.58% (20.238%)	89.374% (1.877%)	86.846% (9.164%)	<b>89.527%</b> (1.827%)	88.54% (6.961%)
Sine2	<b>95.894%</b> (3.055%)	65.559% (27.081%)	76.702% (25.508%)	91.557% (7.497%)	91.593% (9.918%)	<b>94.061%</b> (4.032%)	93.755% (7.22%)
Agr1	<b>90.31%</b> (8.367%)	76.283% (12.768%)	76.282% (10.802%)	87.209% (8.58%)	<b>90.666%</b> (8.733%)	86.706% (8.735%)	88.805% (9.617%)
Agr2	<b>79.528%</b> (10.862%)	67.575% (12.765%)	68.871% (12.383%)	72.668% (10.878%)	<b>81.807%</b> (8.609%)	74.711% (10.684%)	75.038% (12.379%)
Agr3	<b>83.888%</b> (9.128%)	69.972% (8.402%)	70.404% (8.892%)	76.95% (8.428%)	<b>84.499%</b> (8.921%)	77.986% (9.576%)	79.789% (10.644%)
Agr4	<b>80.775%</b> (12.21%)	71.867% (15.6%)	70.141% (14.376%)	78.063% (12.118%)	<b>82.984%</b> (10.584%)	77.679% (11.969%)	78.324% (13.253%)
SEA1	<b>87.569%</b> (1.528%)	86.136% (2.467%)	86.58% (2.974%)	86.434% (1.893%)	<b>87.378%</b> (2.551%)	86.527% (1.633%)	<b>87.538%</b> (1.701%)
SEA2	<b>86.935%</b> (1.761%)	85.05% (3.605%)	85.773% (3.856%)	85.976% (2.514%)	<b>86.953%</b> (2.667%)	85.846% (2.105%)	<b>86.884%</b> (2.08%)
STA1	<b>99.936%</b> (0.223%)	90.324% (11.997%)	90.142% (11.639%)	99.904% (0.291%)	98.129% (5.867%)	<b>99.945%</b> (0.203%)	98.964% (3.343%)
STA2	<b>99.953%</b> (0.156%)	86.898% (15.764%)	87.342% (16.241%)	99.893% (0.3%)	98.004% (6.281%)	<b>99.946%</b> (0.161%)	99.024% (3.2%)

Bold font shows top ranked methods based on Friedman and Nemenyi tests at level of significance of 0.05.

# Accuracy on Real World Data Streams

Data Stream	CDCMS	HTNB	OzaBag	DP	OAUE	RCD	DDD
KDD Cup99	<b>99.738%</b> ( <b>0.191%</b> )	99.65% (0.291%)	<b>99.728%</b> ( <b>0.278%</b> )	99.65% (0.291%)	99.663% (1.073%)	99.65% (0.291%)	99.717% (0.277%)
Power Supply	<b>16.247%</b> ( <b>4.115%</b> )	14.833% (3.359%)	14.907% (3.28%)	14.637% (3.671%)	<b>16.237%</b> ( <b>4.523%</b> )	13.84% (3.226%)	14.838% (3.503%)
Sensor	<b>89.38%</b> ( <b>8.867%</b> )	56.283% (17.35%)	71.126% (15.96%)	83.504% (16.628%)	<b>92.332%</b> ( <b>7.306%</b> )	53.402% (18.793%)	85.838% (12.99%)

Bold font shows top ranked methods based on Friedman and Nemenyi tests at level of significance of 0.05.

# Time Complexity Analysis

- Prediction:

$$O(eM_p)$$

where  $e$  is the ensemble size and  $M_p$  is the base learner prediction time complexity.

- Training:

$$O(eM_t)$$

where  $e$  is the ensemble size and  $M_t$  is the base learner training time complexity.



# Time Complexity Analysis

- **Clustering in the model space** (triggered only when there are concept drift detections):

$O(HbM_p)$  where  $H$  is the memory size,  $b$  is the number of examples in the sliding window, and  $M_p$  is the base learner prediction time complexity.

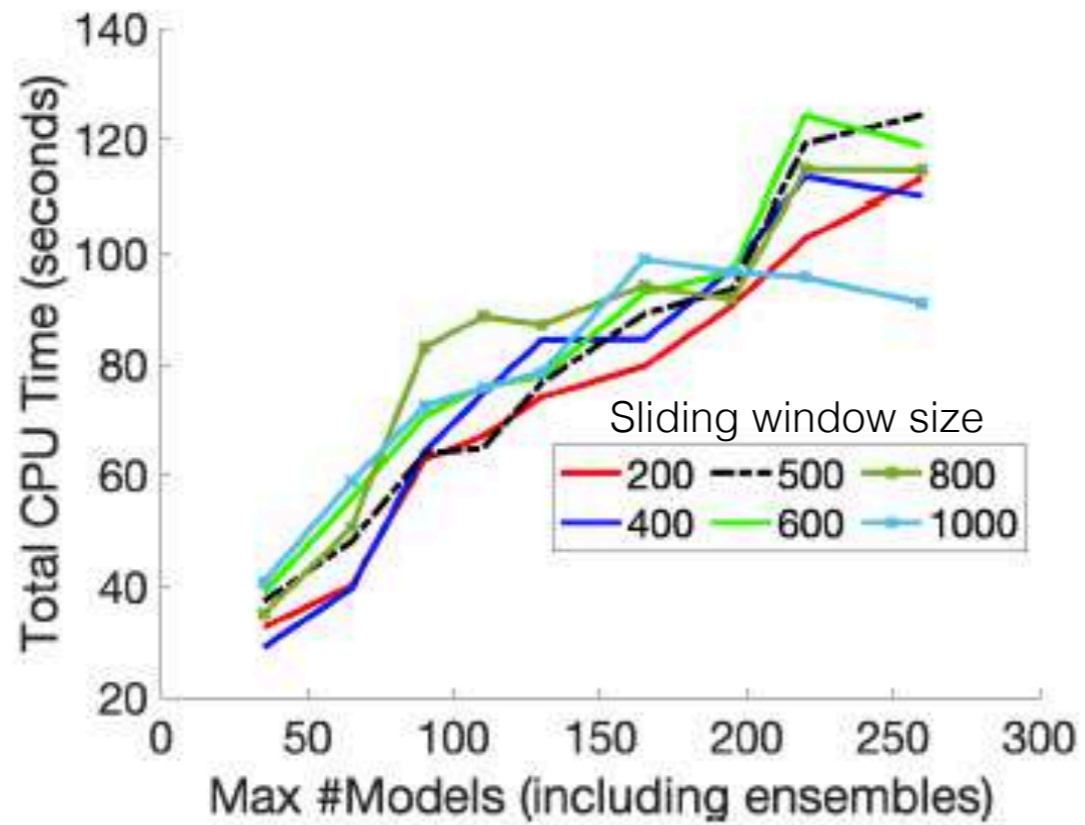
$O(G)$  where  $G$  is the clustering method time complexity.

$O(HbM_p + G)$

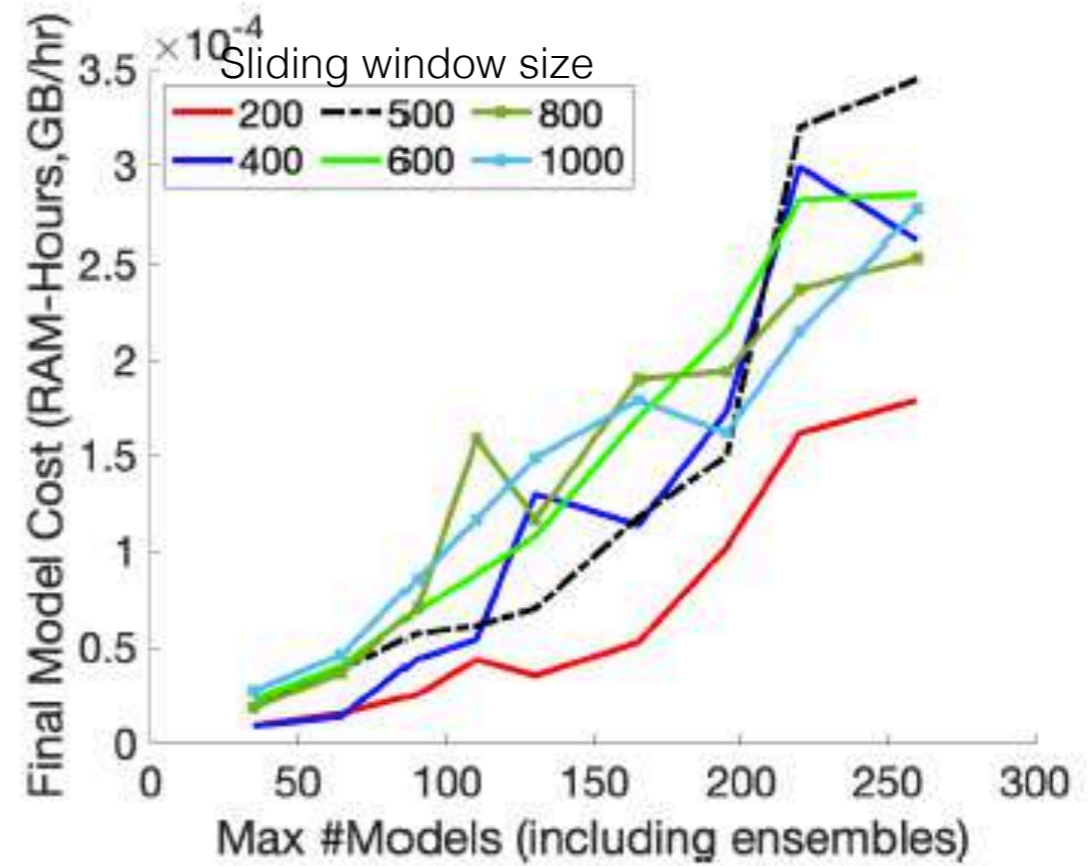
- **Memory management** (triggered at every  $b$  time steps and upon drift detection):

$O(LbM_p)$  where  $L$  is the number of models being compared for diversity,  $b$  is the number of examples in the sliding window and  $M_p$  is the base learner prediction time complexity.

# Runtime and Memory

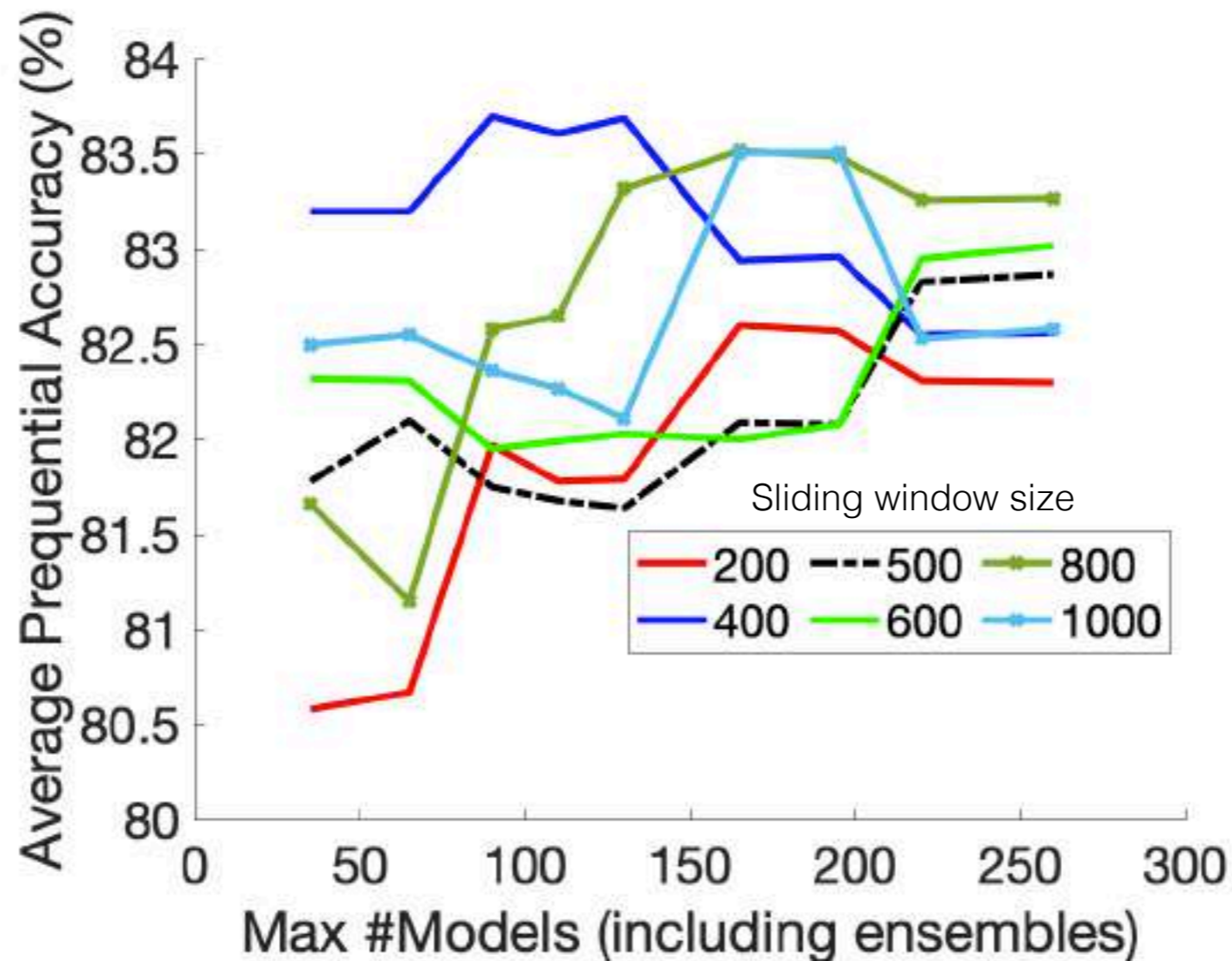


(a) Runtime



(b) Memory

# Accuracy for Different Sliding Window and Maximum Number of Models



(c) Accuracy

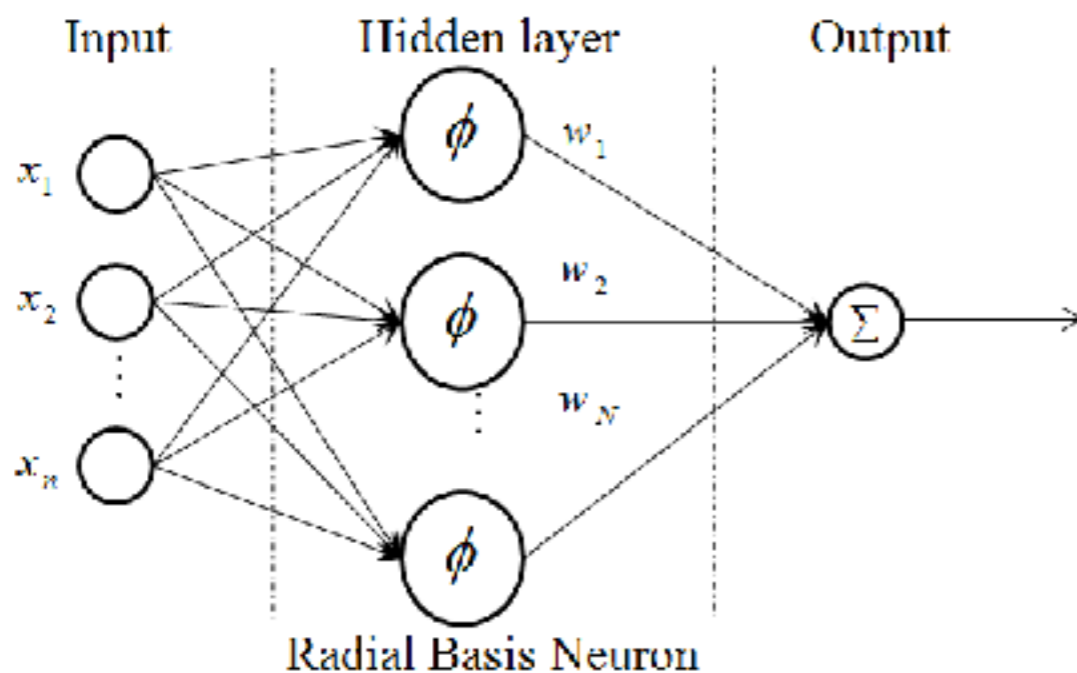
# Conclusions

- Multiple types of concept drift may co-occur in real world problems.
- CDCMS makes use of diversity and clustering in the model space to improve robustness to several different types of drift.
- Most of the time, it successfully managed to recover models from the memory when they are useful to deal with various types of concept drift.
- It successfully created new learners to tackle sudden abrupt drifts that did not involve reoccurrence.

# Other Data Stream Challenges

## - Partially Labelled Data

- Semi-supervised data stream learning.



$$\mathcal{L}(B^{(t)}, \mathbf{w}) = -\frac{1}{L} \sum_{i \in B_l^{(t)}} [y_i \ln(f_i) + (1 - y_i) \ln(1 - f_i)] - \frac{\lambda}{U} \sum_{i \in B_u^{(t)}} [u_i \ln(f_i) + (1 - u_i) \ln(1 - f_i)] + \frac{\alpha}{2N} \|\mathbf{w}\|^2,$$

Automatic adjustment of learning rate to cope with abrupt and gradual drifts.

Closed form solution to learn centres.

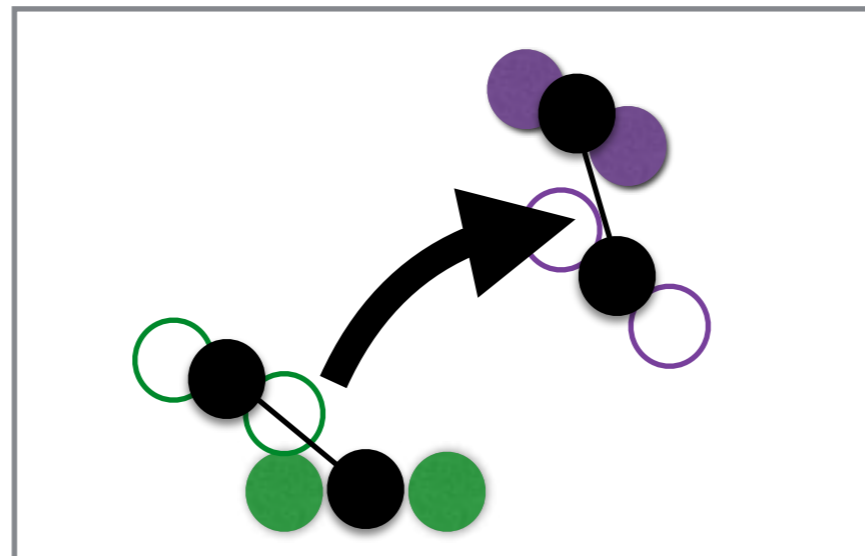
R. Soares and L. Minku. OSNN: An Online Semisupervised Neural Network for Nonstationary Data Streams, [IEEE Transactions on Neural Networks and Learning Systems](#), 2021 (in press).

# Other Data Stream Challenges

## - Small Target Data

- Transfer learning for data streams.

Target data is projected into the source space.



Source models are then used as part of an ensemble to predict the target.

H. Du, L. Minku, H. Zhou. MARLINE: Multi-Source Mapping Transfer Learning for Non-Stationary Environments", [IEEE International Conference on Data Mining](#), 2020.

# Other Data Stream Challenges

## - Verification Latency

- Waiting time strategy with resampling to cope with mislabeled instances.



Implementing a change

We don't know the true label of the change at this stage — that's why we need to predict it.



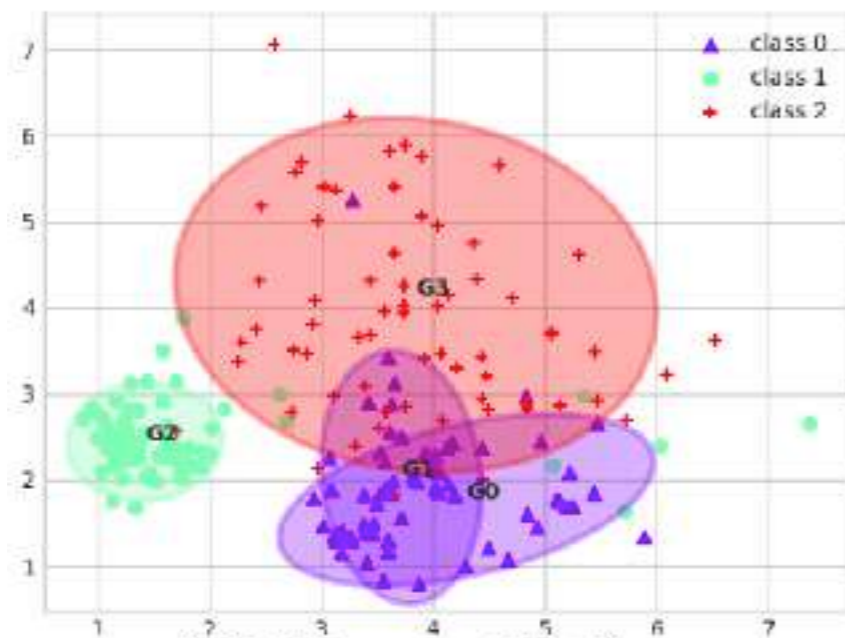
Versioning Repository

Cabral, G.; Minku, L.; Shihab, E.; Mujahid, S. Class Imbalance Evolution and Verification Latency in Just-in-Time Software Defect Prediction. [International Conference on Software Engineering](#), 2019.

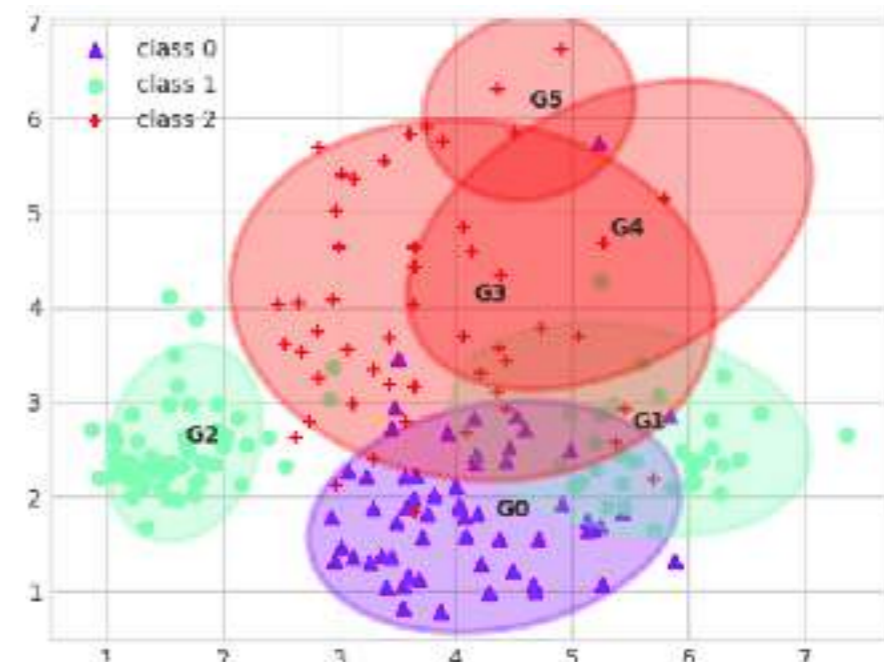
Tabassum, S.; Minku, L.; Feng, D.; Cabral, G.; Song, L. An Investigation of Cross-Project Learning in Online Just-In-Time Software Defect Prediction. [International Conference on Software Engineering](#), 2020.

# Other Data Stream Challenges

- Dealing with concept drifts in  $p^{(t)}(\mathbf{x}, y) = p^{(t)}(y | \mathbf{x})p^{(t)}(\mathbf{x})$



(a) Time: 6050



(e) Time: 6170

Update gaussians for non-severe drifts in  $p(y | \mathbf{x})$

Create gaussians for drifts in  $p(\mathbf{x})$

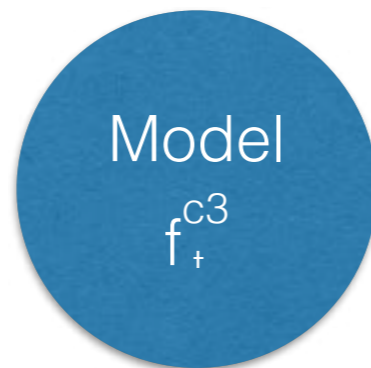
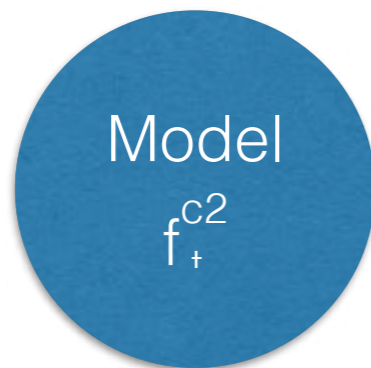
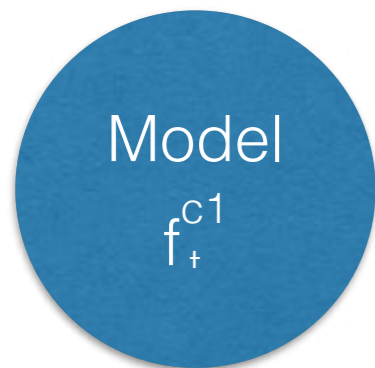
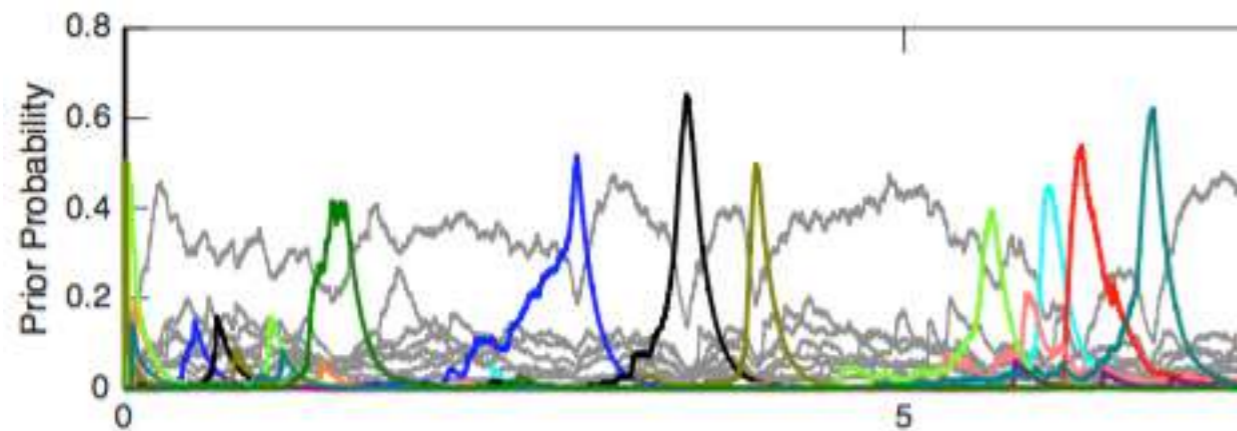
Reset system for severe drifts in  $p(y | \mathbf{x})$

G. Oliveira, L. Minku, A. Oliveira. Tackling Virtual and Real Concept Drifts: An Adaptive Gaussian Mixture Model Approach. [IEEE Transactions on Knowledge and Data Engineering](#), 2021 (in press).



# Other Data Stream Challenges

- Gradual class evolution and class imbalance evolution:




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**Input:** an ensemble with  $M$  base learners, current training example  $(x_t, y_t)$ , and current class size  $w^{(t)} = (w_+^{(t)}, w_-^{(t)})$ .

**for** each base learner  $f_m$  ( $m = 1, 2, \dots, M$ ) **do**

**if**  $y_t = +1$  and  $\begin{cases} w_+^{(t)} < w_-^{(t)} \text{ for OOB} \\ w_+^{(t)} > w_-^{(t)} \text{ for UOB} \end{cases}$

set  $K \sim \text{Poisson}(w_-^{(t)} / w_+^{(t)})$

**else if**  $y_t = -1$  and  $\begin{cases} w_-^{(t)} < w_+^{(t)} \text{ for OOB} \\ w_-^{(t)} > w_+^{(t)} \text{ for UOB} \end{cases}$

set  $K \sim \text{Poisson}(w_+^{(t)} / w_-^{(t)})$

**else**

set  $K \sim \text{Poisson}(1)$

**end if**

update  $f_m$   $K$  times

**end for**

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Sun et al. Online Ensemble Learning of Data Streams with Gradually Evolved Classes, [IEEE Transactions on Knowledge and Data Engineering](#) 28(6):1532–1545, 2016.

S. Wang, L. Minku, X. Yao. Resampling-Based Ensemble Methods for Online Class Imbalance Learning, [IEEE Transactions on Knowledge and Data Engineering](#) 27(5): 1356-1368, 2015.

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